



UNIVERSITY EXAMINATIONS

RESIT/SPECIAL

EXAMINATION FOR THE AWARD OF DEGREE OF BACHELOR OF SCIENCE,
BACHELOR OF EDUCATION AND BACHELOR OF ARTS

MATH 241: PROBABILITY AND STATISTICS I

STREAMS: BSC, BED (ARTS)

TIME: 2 HOURS

DAY/DATE: TUESDAY 02/02/2021

2.30 P.M. – 4.30 P.M.

INSTRUCTION: Answer ALL the Questions

QUESTION ONE (30 MARKS)

- a) Distinguish between the following probability mass function and a probability density function (2 marks)
- b) A discrete random variable has the following p.m.f.

x	3	4	5	6	7
$Pv(X = x)$	0.1	a	0.3	b	0.2

If $E(x) = 5.2$.

Find the

- i) values of 'a' and 'b' (4 marks)
- ii) The $\text{Var}(x)$ (3 marks)
- iii) Cdf of the random variable (2 marks)
- c) A random variable has the exponential distribution

$$f(x) = \begin{cases} \lambda e^{-\lambda x}; & x > 0 \\ 0 & \text{otherwise} \end{cases}$$

- i) Show that the moment generating function is

$$M_x(t) = \left(1 - t/\lambda\right)^{-1} \quad (4 \text{ marks})$$

- ii) Hence find the mean and variance of x. (7 marks)

MATH 241

d) If $f(x) = b(x; n, p)$, $E(x) = 4$, $\text{var}(x) = 3$. Compute $\Pr(x \geq 1)$ (3 marks)

e) A random variable x is normally distributed with $\mu = 20$ and $\sigma^2 = 16$. If

$$Y = \frac{1}{4}(x - 20)$$

Find

i) $E(Y)$

ii) $\text{Var}(Y)$

iii) Hence or otherwise write down the p.d.f. of Y . (5 marks)

QUESTION TWO (20 MARKS)

a) Let Y be a continuous random variable. Show that the function

$$f(y) = \begin{cases} \frac{y}{2} & 0 \leq y \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

Is indeed a probability density function.

(2 marks)

Hence determine

i) $\Pr(-1 \leq y \leq 1)$

(3 marks)

ii) $E(y)$

(3 marks)

iii) The cumulative distribution function $F(y)$

(3 marks)

b) Give $f(x)$ is a Poisson distribution function of r.v x , show that it's moment

generating function is given by $m_x(t) = e^{\lambda(e^t - 1)}$. Hence or otherwise determine the

mean of x .

(9 marks)

QUESTION THREE (20 MARKS)

a) The annual number of earthquakes registering at least 2.5 on the Richter Scale

and having an epicenter within 40 miles of downtown Memphis follows a

Poisson distribution with mean 6.5. What is the probability that at least 9 such

earthquakes will strike next year?

(5 marks)

b) Let X be a Bernoulli random variable with probability mass function given by;

$$\begin{cases} p^x(1-p)^{1-x}, x = 0,1 \\ 0, \text{ otherwise} \end{cases}$$

MATH 241

Find;

- i) The factorial moment generating (5 marks)
 - ii) The probability generating function (5 marks)
 - iii) The mean and variance (5 marks)
-