



**FIRST YEAR EXAMINATIONS FOR BACHELOR OF SCIENCE, COMPUTER SCIENCE & APPLIED COMPUTER SCIENCE**

**COSC 102: DISCRETE STRUCTURES**

**STREAMS: BSC (COMP SCI & APPLIED COMP. SCI) Y1S2**

**TIME 2 HOURS**

**DAY/DATE: WEDNESDAY 10/4/2019**

**8.30 A.M. – 10.30 A.M.**

**INSTRUCTIONS**

- Answer **QUESTION 1** and any other **TWO QUESTIONS** from section B.
- This is a **CLOSED BOOK EXAM**, No reference materials allowed in examination room. Mobile phones must be switched off.
- Do not write on this question paper
- Write your answers legibly and use your time wisely.
- Scientific, non-programable Calculators may be used.

**SECTION A: COMPULSORY**

**QUESTION 1[30MKS]**

- a) What is the Cartesian product of  $A = \{1, 2\}$  and  $B = \{a, b\}$ ? [4 marks]
- b) Determine the members of the set  $S = \{x \mid x \text{ is the square of an integer and } x < 100\}$  [4 marks]
- c) Let  $p$  be a proposition,  $P : I \text{ am in Student.}$ ,  $Q : I \text{ love football.}$  What is  $p \rightarrow q$  (q implies p)? [2 marks]
- d) Suppose there are 50 people in a room, how many of them must have their birthday in the same month? [4 marks]
- e) Construct the Truth table of the following compound proposition  
 $(P \vee \neg Q) \rightarrow (P \wedge Q)$  [6 marks]
- f) Given that variable names in a programming language can be either a single uppercase letter or an uppercase letter followed by a digit, find the number of possible variable names [4 marks]
- g) How many bit strings of length 8 either start with a 1 or end with two bits 00? [2 marks]

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- h) Suppose a list A contains the 30 students in a mathematics class, and a list B contains the 35 students in an English class, and suppose there are 20 names on both lists. Find the number of students:
- (i) Only on list A, (ii) only on list B, (iii) on list A or B (or both), (iv) on exactly one list. [4 marks]

### SECTION B: ATTEMPT ONLY TWO QUESTIONS FROM THIS SECTION

#### Question 2 [20mks]

With the use of direct proof or otherwise, prove the following:

- (a) The square of an even natural number is even [6 marks]
- (b) The square of an odd natural number is odd [4 marks]
- (c) The claim that if  $n$  is a positive integer, then the quantity  $n^2+3n+2$  is even [4 marks]
- (d) With the use of relevant examples, discuss proof by induction [6 marks]

#### Question 3[20mks]

- (a) Find the number of permutations of six objects, {A,B,C,D,E,F} taking three at a time [8 marks]
- (b) A farmer buys 3 cows, 2 pigs and 4 hens from a man who has 6 cows, 5 pigs, and 8 hens. Find the number of choices the farmer has to make [12 marks]

#### Question 4[20mks]

- (a) Let M, P and C be the sets of students taking Mathematics, Physics and Computer courses respectively in Chuka University. Take  $|M| = 300$ ,  $|P| = 350$ ,  $|C| = 450$ ,  $|M \cap P| = 100$ ,  $|M \cap C| = 150$ , and  $|P \cap C| = 75$ ,  $|M \cap P \cap C| = 10$ . Determine the number of students taking exactly one of the above courses. [12 marks]
- (b) Mingingo highland has two kinds of inhabitants, knights and knaves. Knights always tell the truth, and only the truth; Knaves always tell lies, and only lies. John encountered two people on his visit to the highland, A and B. Determine what is A and B if A tells John “B is a Knight” and B “says The two of us are of opposite type” [8 marks]

#### Question 5 [20mks]

- (a) Find the number M of seven letter words that can be formed using the word “BENZENE”. [8 marks]
- (b) Use Binomial theorem to Determine the coefficient of  $x^{12}y^{13}$  in the expansion of  $(x+y)^{25}$  [4 marks]
- (c) Determine the expansion of  $(x+y)^4$  using Binomial theorem [8 marks]