

CHUKA**UNIVERSITY****UNIVERSITY EXAMINATIONS****CHUKA AND THARAKA CAMPUSES**

**FIRST YEAR EXAMINATION FOR THE AWARD OF DEGREE OF
BACHELOR OF SCIENCE (ACTUAL SCIENCE)**

ACMT 111: COMPUTATIONAL METHOD AND DATA ANALYSIS I**STREAMS:****TIME: 2 HOURS****DAY/DATE: WEDNESDAY 08/04/2020****2.30 P.M. – 4.30 P.M.****INSTRUCTIONS**

- Answer questions **ONE** (compulsory) and any other **TWO** questions

QUESTION ONE (30 MARKS)

- a) Following is a table of values for $f(x) = \tan x$ for a few values of x

x	1	1.1	1.2	1.3
$\tan x$	1.5574	1.9648	2.5722	3.6021

Use linear interpolation to estimate $\tan(1.15)$.

(5 marks)

- b) A statistical survey is implemented according to a series of steps each of which includes a specific and defined set of formats and procedures. Highlight eight such of statistical survey implementation (4 marks)

- c) Consider the function

$$U(x) = x^2$$

Find the first order forward finite difference approximation to $U_x(3)$ using step size $h = 0.1$

(5 marks)

- d) Given a relative error $r.e. = 0.5$, how many significant digits do we have?

(3 marks)

- e) State five important uses of Statistical Package for Social Science in modern days data analysis
(5 marks)
- f) Discuss three type of error commonly used in numerical computations
(3 marks)
- g) Explain five importance use of the advanced technology in complex data analysis
(5 marks)

QUESTION TWO (20 MARKS)

- a) Using finite difference method solve the following differential equation

$$\frac{d^2 x(t)}{dt^2} + x(t) = 0$$

$$\text{With } x(0) = 1 \text{ and } x(0) = 0$$

(10 marks)

- b) By finite difference approximate the solution of the initial-value problem

$$y'' - \left(1 - \frac{x}{5}\right)y = x$$

$$y(1) = 2 \text{ and } y(3) = -1$$

on the interval $1 \leq x \leq 3$.

(10 marks)

QUESTION THREE (20 MARKS)

- a) Define databases
(2 marks)
- b) Describe six purposes of databases system in modern day society
(6 marks)
- c) Describe the importance of data integrity, security, and privacy and how they affect database design.
(8 marks)
- d) State four areas where databases are mostly applicable
(4 marks)

QUESTION FOUR (20 MARKS)

Approximate the solution of the nonlinear ordinary differential equation

$$8y'' + yy' = 2x^3 + 32$$

$$\text{Where } y(1) = 17 \text{ and } y(4) = 45$$

(20 marks)

QUESTION FIVE (20 MARKS)

a) Consider the following tables of functions values generated with $f(x) = \ln x$

i	x_i	f_i
0	0.40	-0.916291
1	0.50	-0.693147
2	0.70	-0.356675
3	0.80	-0.223144

Find $g(0.60)$

(10 marks)

b) Refer to the data in the following table. Interpolate the data from $x = 1$ to 10 at increments of 0.5 using linear interpolation. Plot the interpolated values and data together using each of the following methods (create a new plot with the data for each method). Label your axis on the plots.

x	1	2	3	4	6	8	10
y	2	2.5	7	10.5	12.75	13	13

Use a 3rd order Lagrange interpolating polynomial to predict y at $x = 1.25$ for the following data

x	y
1	0.14
1.1	0.21
1.2	0.33
1.3	0.54
1.4	0.92

(10 marks)